## Mechanics M1 Mark scheme

## Question

1
$\left.\begin{array}{|l|l|l|}\hline 76=4 u+\frac{1}{2} a .4^{2} \text { or } \\ 76=\frac{1}{2}(u+\overline{u+4 a}) \times 4\end{array} \quad \begin{array}{l}\text { Use of } s=u t+\frac{1}{2} a t^{2} \text { for } \\ t=4, s=76 \text { and } u \neq 0 \text { (use } \\ \text { of } u=0 \text { is M0) }\end{array}\right)$ M1

## Alternative

| $t=2, v_{2}=\frac{76}{4}=19$ | Find the speed at $t=2, t=7$ <br> $t=7, v_{7}=\frac{219}{6}=36.5$ <br> Both values correct <br> Averages with no links to times is <br> M0 | M1 |
| :---: | :--- | :---: |
| A1 |  |  |
| $36.5=19+5 a \Rightarrow a=3.5$ | Use of $v=u+5 a$ with their $u, v$ <br> Correct $a$ | M1 |
| A1 |  |  |
| $19=u+2 a$ | Complete method for finding $u$ <br> Correct equation in $u$ | DM1 |
| A1 |  |  |
| $u=19-7=12$ |  | A 1 |


| Question | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 2(a) | $\begin{aligned} & m u-2 k m u=-\frac{1}{2} m u+k m u \\ & \text { or } \\ & m\left(\frac{1}{2} u+u\right)=-k m(-u-2 u) \end{aligned}$ | Use of CLM or Equal and opposite impulses Need all 4 terms dimensionally correct. <br> Masses and speeds must be paired correctly <br> Condone sign errors <br> Condone factor of g throughout. | M1 |
|  | Unsimplified equation with at most one error |  | A1 |
|  | Correct unsimplified equation |  | A1 |
|  | $k=\frac{1}{2}$ | From correct working only | A1 |
|  |  |  | (4) |
| (b) | For $P: I= \pm m\left(\frac{1}{2} u \pm-u\right)$ <br> For $\mathrm{Q}: I= \pm k m(u \pm-2 u)$ | Impulse on $P$ or impulse on $Q$. <br> Mass must be used with the correct speeds <br> e.g. $k m \times \frac{1}{2} u$ is M 0 <br> If working on $Q$, allow equation using <br> their $k$. <br> Terms must be dimensionally correct. <br> Use of g is M0 | M1 |
|  | $\frac{3 m u}{2}$ | Only <br> From correct working only | A1 |
|  |  |  | (2) |
| (6 marks) |  |  |  |


| 3(a) | $7^{2}=2 \times 9.8 h$ | Use of $v^{2}=u^{2}+2 a s$ with $u=0, v=7$ <br> or alternative complete method to find $h$ | M1 |
| :---: | :---: | :---: | :---: |
|  | $h=2.5$ | Condone $h=-2.5$ in the working but the final answer must be positive. | A1 |
|  |  |  | (2) |
| (b) | $9 \times 7=10.5 u$ | Use CLM to find the speed of the blocks after the impact. Condone additional factor of g throughout. | M1 |
|  | $u=6$ |  | A1 |
|  | $0^{2}=6^{2}-2 a \times 0.12$ | Use of $v^{2}=u^{2}+2 a s$ with $u=6, v=0$ <br> Allow for their $u$ and $v=0$ <br> Allow for $u=7, v=0$ <br> Accept alternative suvat method to form an equation in $a$. <br> Condone use of 12 for 0.12 | M1 |
|  |  | Correctly substituted equation in $a$ with $u=6, s=0.12$ <br> (implied by $a=150$ ) | A1 |
|  | ( $\downarrow$ ) $10.5 g-R=10.5 \times(-\mathrm{a})$ | Use of $F=m a$ with their $a \neq \pm \mathrm{g}$. <br> Must have all 3 terms and 10.5 <br> Condone sign error(s) | M1 |
|  | ( $\downarrow$ ) $10.5 g-R=10.5 \times(-150)$ | Unsimplified equation with $a$ substituted and at most one error (their $a$ with the wrong sign is 1 error) | A1 |
|  |  | Correct unsimplified equation with $a$ substituted | A1 |
|  | $R=1680$ or 1700 |  | A1 |
|  |  |  | (8) |
|  | Alternative for the last 6 marks: |  |  |
|  | $\frac{1}{2} \times 10.5 \times 6^{2}+10.5 \times 9.8 \times 0.12=R \times 0.12$ | Energy equation ( needs all three terms) | M2 |
|  |  | -1 each error A1A1A0 for 1 error, A1A0A0 for 2 errors | A3 |
|  | R=1680 or 1700 |  | A1 |


| 4(a) |  |  |  |
| :---: | :---: | :---: | :---: |
|  | $M(A)(30 \mathrm{~g} \times 2)+(50 \mathrm{gx} 4)=0.6 S$ $M(C) \quad(0.6 \times R)=(1.4 \times 30 \mathrm{~g})+(3.4 \times 50 \mathrm{~g})$ <br> $M(G) \quad(2 \times R)=(1.4 \times S)+(2 \times 50 \mathrm{~g})$ $M(B)(4 \times R)+(2 \times 30 g)=(3.4 \times S)$ | Moments equation. Requires all terms and dimensionally correct. Condone sign errors. <br> Allow M1 if g missing | M1 |
|  |  | Correct unsimplified equation | A1 |
|  | $\begin{aligned} & \text { (१) } R+30 g+50 g=S \\ & (R+784=S) \end{aligned}$ | Resolve vertically. Requires all 4 terms. Condone sign errors | M1 |
|  | Correct equation (with $R$ or their $R$ ) <br> NB: The second M1A1 can also be earned for a second moments equation |  | A1 |
|  | $R=3460 \text { or } 3500 \text { or } \frac{1060 g}{3}(\mathrm{~N})$ <br> Not 353.3g $\begin{equation*} S=4250 \text { or } 4200 \text { or } \frac{1300 g}{3} \tag{N} \end{equation*}$ <br> Not 433.3g | One force correct | A1 |
|  |  | Both forces correct <br> If both forces are given as decimal multiples of $g$ mark this as an accuracy penalty A0A1 | A1 |
|  |  |  | (6) |
| (b) | $M(C)\left(30 \mathrm{~g} \mathrm{x} \mathrm{1.4)+(Mg} \mathrm{\times 3.4)=0.6} \mathrm{\times 50} \mathrm{and} \mathrm{dimensionally} \mathrm{correct}. \begin{array}{l}\text { Use } R=5000 \text { and complete } \\ \text { method to form an equation in } M \\ \text { or weight. Needs all terms present } \\ \text { Condone sign errors. } \\ \text { Accept inequality. } \\ \text { Use of } R \text { and } S \text { from (a) is M0 }\end{array}\right.$ |  | M1 |
|  |  | Correct equation in $M$ (not weight) (implied by $M=77.68$ ) | A1 |
|  | $M=77 \mathrm{~kg}$ | 77.7 is A 0 even is the penalty for over-specified answers has already been applied | A1 |
|  |  |  | (3) |


| Question | Scheme | Marks |  |
| :---: | :--- | :--- | :---: |
| 4(c) | The weight of the diver acts at a point. | Accept "the mass of the diver is at <br> a point". | B1 |
|  |  | (1) |  |


| Question | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 5(a) | $(2 \mathbf{i}-3 \mathbf{j})+(p \mathbf{i}+q \mathbf{j})=(p+2) \mathbf{i}+(q-3) \mathbf{j}$ | Resultant force $=\mathbf{F}_{1}+\mathbf{F}_{2}$ in the form $a \mathbf{i}+b \mathbf{j}$ | M1 |
|  | $\frac{p+2}{q-3}=\frac{1}{2} \quad$ or $\left.\quad \begin{array}{c}p+2=n \\ q-3=2 n\end{array}\right\}$ for $n \neq 1$ | Use parallel vector to form a scalar equation in $p$ and $q$. | M1 |
|  |  | Correct equation (accept any equivalent form) | A1 |
|  | $4+2 p=-3+q$ | Dependent on no errors seen in comparing the vectors. <br> Rearrange to obtain given answer. <br> At least one stage of working between the fraction and the given answer | DM1 |
|  | $2 p-q+7=0$ | Given Answer | A1 |
|  |  |  | (5) |
| 5(b) | $q=11 \Rightarrow p=2$ |  | B1 |
|  | $\mathbf{R}=4 \mathbf{i}+8 \mathbf{j}$ | $(2+p) \mathbf{i}+8 \mathbf{j}$ for their $p$ | M1 |
|  | $4 \mathbf{i}+8 \mathbf{j}=2 \mathbf{a} \quad(\mathbf{a}=2 \mathbf{i}+4 \mathbf{j})$ | Use of $\mathbf{F}=m \mathbf{a}$ | M1 |
|  | $\|\mathbf{a}\|=\sqrt{2^{2}+4^{2}}$ | Correct method for $\|\mathbf{a}\|$ <br> Dependent on the preceding M1 | DM1 |
|  | $=\sqrt{20}=4.5$ or 4.47 or better $\left(\mathrm{m} \mathrm{s}^{-2}\right)$ | $2 \sqrt{5}$ | A1 |
|  |  |  | (5) |
|  | Alternative for the last two M marks: |  |  |
|  | $\|\mathbf{F}\|=\sqrt{16+64}(=\sqrt{80})$ | Correct method for $\|\mathbf{F}\|$ | M1 |
|  | $\sqrt{80}=2 \times\|\mathbf{a}\|$ | Use of $\|\mathbf{F}\|=m\|\mathbf{a}\|$ <br> Dependent on the preceding M1 | DM1 |
|  |  |  | (5) |


| Question | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 6(a) | $v=u+a t \Rightarrow 14=3.5 a$ | Use of suvat to form an equation in $a$ | M1 |
|  | $a=4$ |  | A1 |
|  |  |  | (2) |
| (b) |  | Graph for $A$ or $B$ | B1 |
|  |  | Second graph correct and both graphs extending beyond the point of intersection | B1 |
|  |  | Values $3.5,14, T$ shown on axes, with $T$ not at the point of intersection. Accept labels with delineators. | B1 |
|  | NB: 2 separate diagrams scores max B1B0B1 |  | (3) |
| (c) | $\frac{1}{2} T .3 T, \quad \frac{(T+T-3.5)}{2} .14$ | Find distance for A or B in terms of $T$ only. <br> Correct area formulae: must see $\frac{1}{2}$ in area formula and be adding in trapezium | M1 |
|  | One distance correct |  | A1 |
|  | Both distances correct |  | A1 |
|  | $\begin{aligned} \frac{1}{2} T .3 T & =\frac{(T+T-3.5)}{2} .14 \\ \frac{1}{2} T .3 T & =\frac{1}{2} \times 4 \times 3.5^{2}+14(T-3.5) \end{aligned}$ | Equate distances and simplify to a 3 term quadratic in $T$ in the form $a T^{2}+b T+c=0$ | M1 |
|  | $3 T^{2}-28 T+49=0$ | Correct quadratic | A1 |
|  | $(3 T-7)(T-7)=0$ | Solve 3 term quadratic for $T$ | M1 |
|  | $T=\frac{7}{3}$ or 7 | Correct solution(s) - can be implied if only ever see $T=7$ from correct work. | A1 |
|  | but $T>3.5, \quad T=7$ |  | A1 |
|  |  |  | (8) |
| (d) | 73.5 m From correct work only. B0 if <br> extra answers. |  | B1 |
|  |  |  | (1) |


| Question |
| :---: | :---: | :--- | :--- | :--- |
| 6(e) |


| Question | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 7(a) | $F=0.25 R$ |  | B1 |
|  | $\begin{aligned} & \sin \alpha=\frac{3}{5} \text { or } \cos \alpha=\frac{4}{5} \\ & \sin \beta=\frac{4}{5} \text { or } \cos \beta=\frac{3}{5} \end{aligned}$ | Use of correct trig ratios for $\alpha$ or $\beta$ | B1 |
|  | $\begin{aligned} & \text { (31.36) } \end{aligned} \quad R=4 g \cos \alpha$ | Normal reaction on $P$ <br> Condone trig confusion (using $\alpha$ ) | M1 |
|  |  | Correct equation | A1 |
|  | $T+F=4 g \sin \alpha$ | Equation of motion for $P$. Requires all 3 terms. <br> Condone consistent trig confusion <br> Condone an acceleration not equated to 0 : $T+F-4 g \sin \alpha=4 a$ | M1 |
|  | $\begin{aligned} & (T+7.84=23.52) \\ & (T=15.68) \end{aligned}$ | Correct equation | A1 |
|  | $T=m g \sin \beta$ | Equation of motion for $Q$ <br> Condone trig confusion <br> Condone an acceleration not equated to 0 : $T-m g \sin \beta=-m a$ | M1 |
|  | ( $T=7.84 m$ ) | Correct equation | A1 |
|  | Solve for $m$ | Dependent on the 3 preceding M marks <br> Not available if their equations used $a \neq 0$ | DM1 |
|  | $m=2$ |  | A1 |
|  | NB Condone a whole system equation $4 g \sin \alpha-F=m g \sin \beta$ followed by $m=2$ for $6 / 6$ <br> M2 for an equation with all 3 terms. Condon trig confusion. Condone an acceleration $\neq 0$ <br> A2 (-1 each error) for a correct equation: |  |  |
|  |  |  | (10) |
| 7(b) | $\begin{gathered} F=\sqrt{T^{2}+T^{2}} \text { or } 2 T \cos 45^{\circ} \text { or } \\ \frac{T}{\cos 45} \end{gathered}$ | Complete method for finding $F$ in terms of $T$ <br> Accept $\sqrt{\left(R_{h}\right)^{2}+\left(R_{v}\right)^{2}}$ | M1 |
|  | Correct expression in $T$ |  | A1 |
|  | Substitute their $T$ into a correct expression. Dependent on the previous M mark |  | DM1 |
|  | $F=\sqrt{2} \frac{8 g}{5}=22 \text { or } 22.2(\mathrm{~N})$ | Watch out - resolving vertically is not a correct method and gives 21.9 N . | A1 |
|  |  |  | (4) |


| Question | Scheme | Marks |  |
| :---: | :--- | :--- | :---: |
| $\mathbf{7 ( c )}$ | Along the angle bisector at the <br> pulley | Or equivalent - accept angle + arrow <br> shown on diagram. <br> $\left(8.1^{\circ}\right.$ to downward vertical $)$ <br> Do not accept a bearing |  |
|  |  | $(\mathbf{1 5}$ marks) |  |

